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# Discrete Control Systems in LabVIEW

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- PID Controller
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  - We make a basic Control System where the Discrete Model and Discrete PI Controller are used



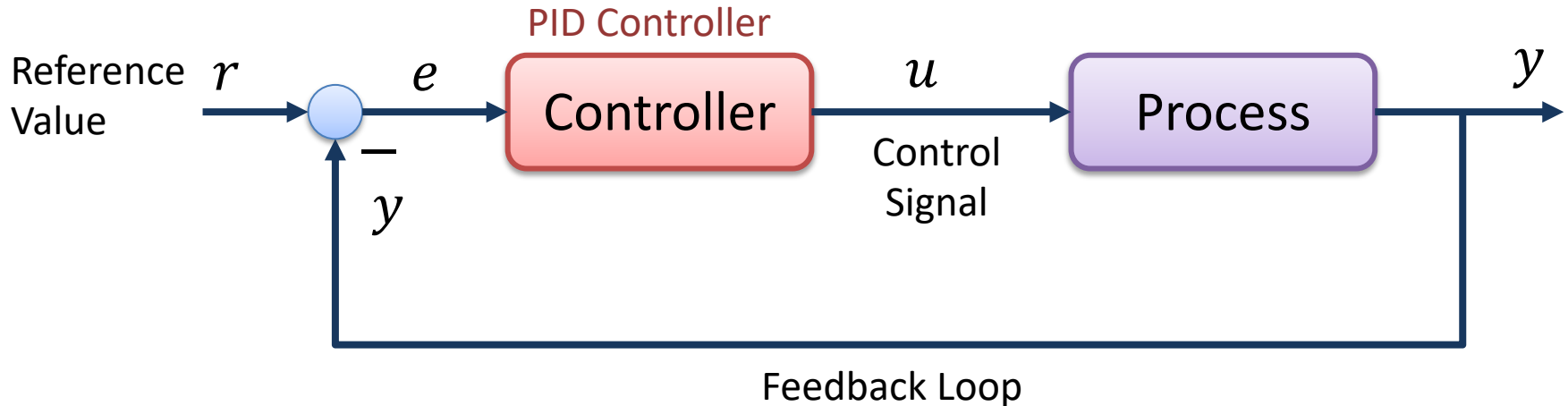
# Introduction

# Introduction

- We will simulate a 1. Order Process/Differential Equation
  - We will Implement a Discrete version of the Model and perform Simulations
- We will create a basic Control System
  - We will make and Implement a Discrete PI Controller and perform Simulations

# Control System

The purpose with a Control System is to Control a Dynamic System, e.g., an industrial process, an airplane, a self-driven car, etc. (a Control System is “everywhere” today)





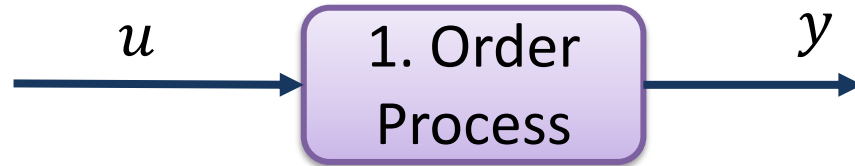
# Mathematical Model

# 1. Order System

Differential Equation of a 1. order System:

$$\dot{x} = -ax + bu$$

$$y = x$$



In order to simulate this model in LabVIEW you can make a discrete version of the model, or you can implement it as a “Block Diagram” using the features in LabVIEW Control Design and Simulation Module

# 1. Order System

Assume the following general **Differential Equation**:

$$\dot{y} = -ay + bu$$

or:

$$\dot{y} = \frac{1}{T}(-y + Ku)$$

$$\text{Where } a = \frac{1}{T} \text{ and } b = \frac{K}{T}$$



Where  $K$  is the Gain and  $T$  is the Time constant

This differential equation represents a 1. order dynamic system

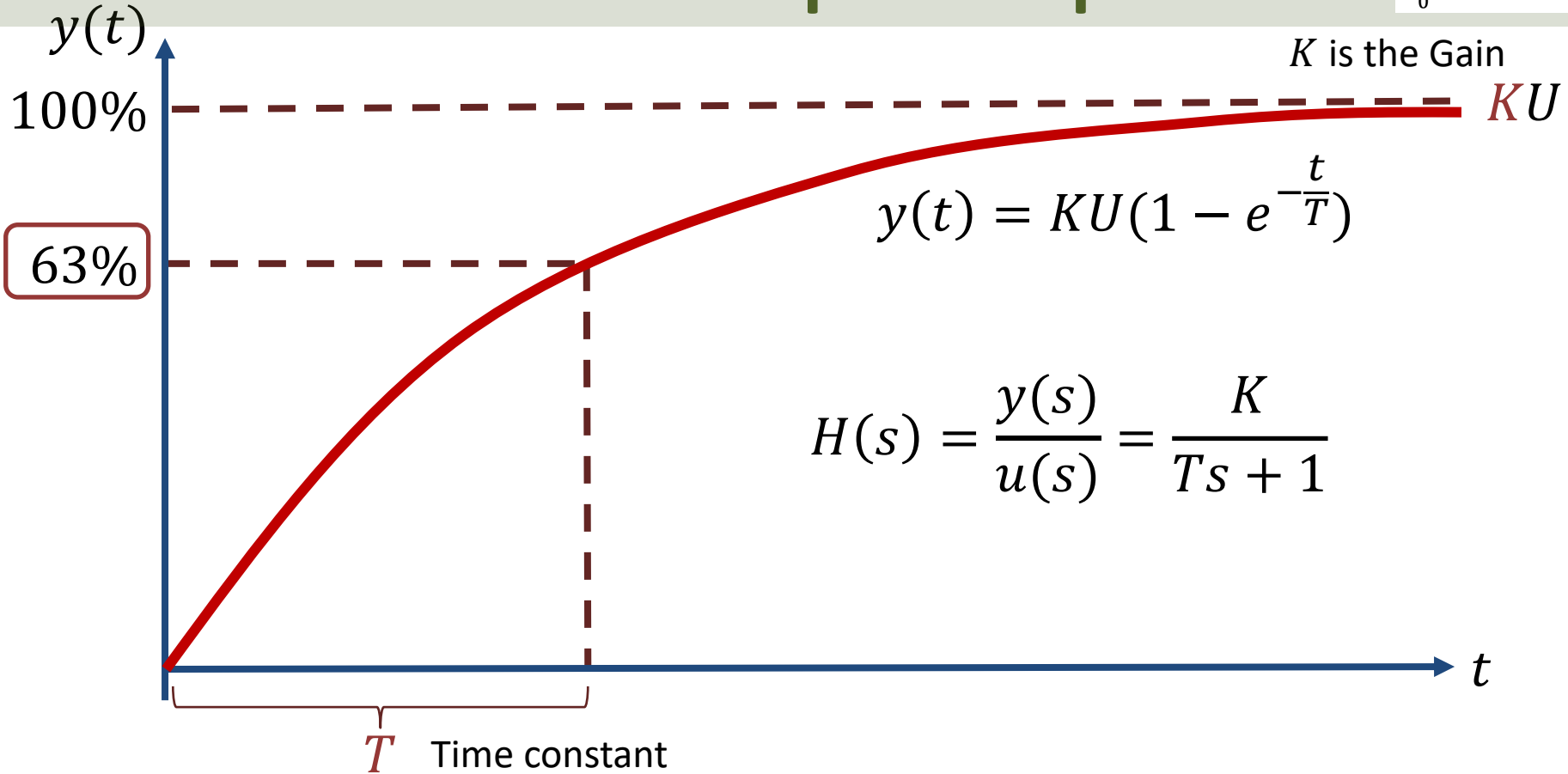
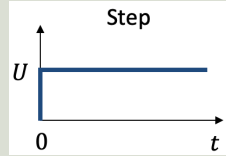
Assume  $u(t)$  is a step ( $U$ ), then we can find that the solution to the differential equation is:

$$y(t) = KU(1 - e^{-\frac{t}{T}})$$

(by using Laplace)



# 1. Order Step Response



# Discretization

We have the continuous differential equation:  $\dot{x} = -ax + bu$

We apply **Euler**:  $\dot{x} \approx \frac{x(k+1) - x(k)}{T_s}$

Then we get:

$$\frac{x(k+1) - x(k)}{T_s} = -ax(k) + bu(k)$$

This gives the following discrete differential equation (difference equation):

$$x(k+1) = (1 - T_s a)x(k) + T_s bu(k)$$

This equation can easily be implemented in any text-based programming language or the Formula Node in LabVIEW

Where  $a = \frac{1}{T}$  and  $b = \frac{K}{T}$

# Discrete Model in LabVIEW

$$x(k + 1) = (1 - T_s a)x(k) + T_s b u(k)$$

Discrete Model2.vi Front Panel

File Edit View Project Operate Tools Window Help

24pt Application Font

U: 1

Process Value [°C]: 8.00

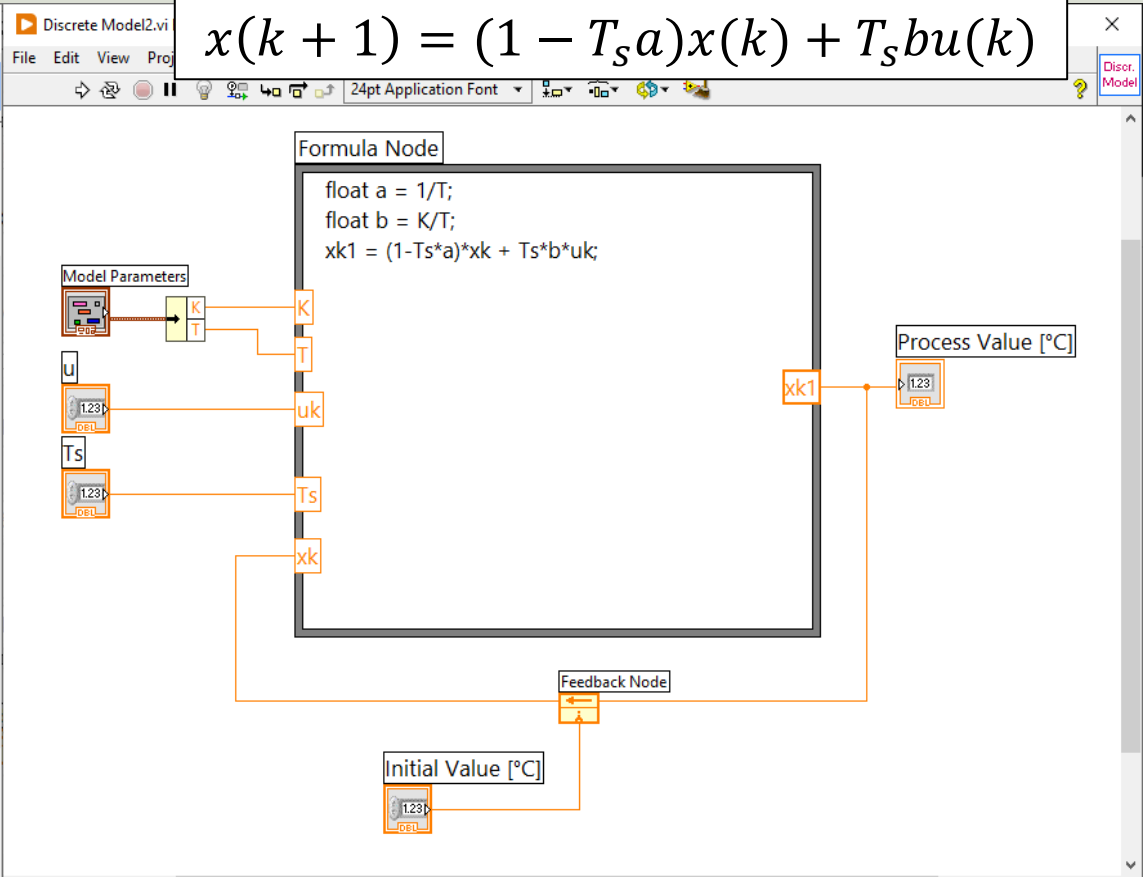
Initial Value [°C]: 0.00

Model Parameters

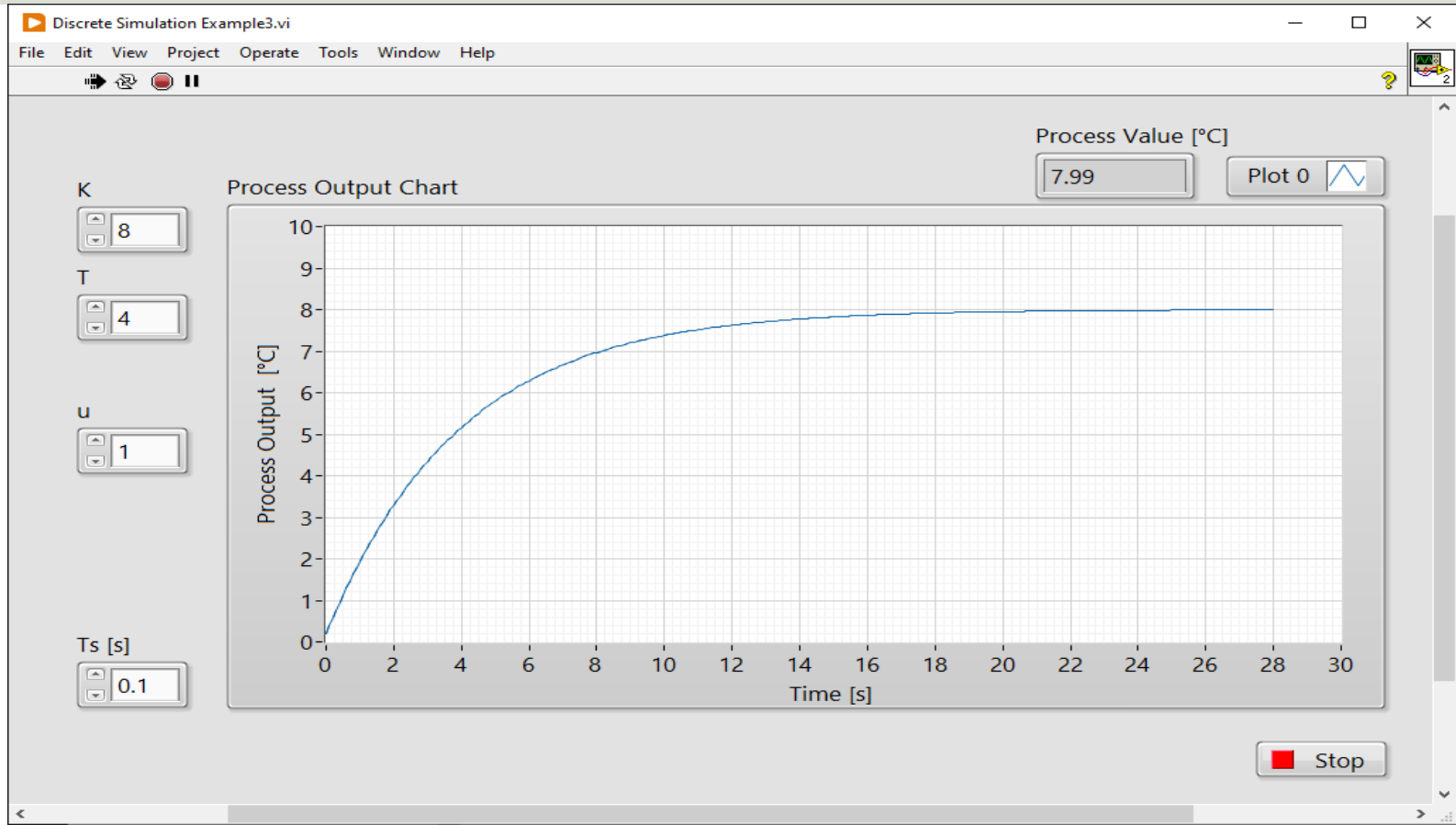
K: 8

T: 4

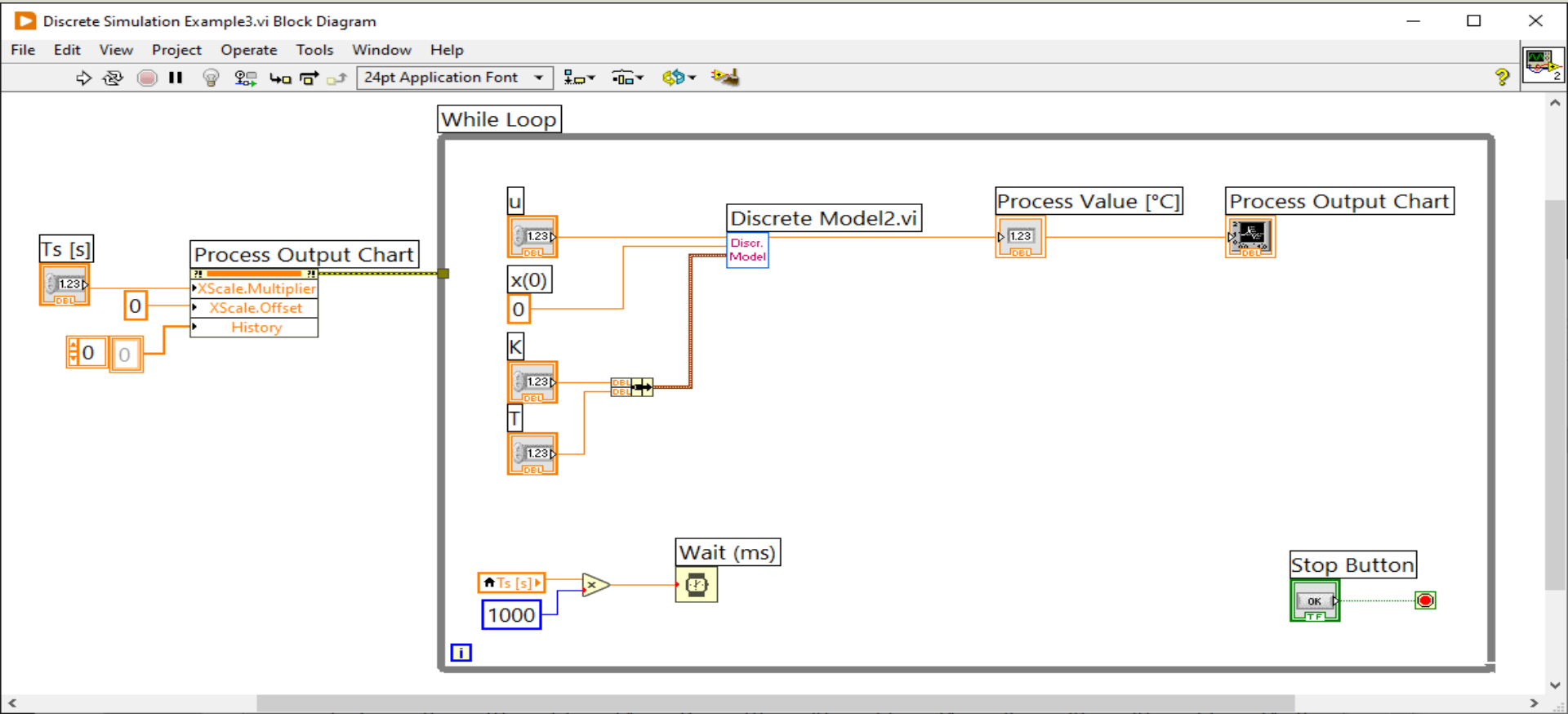
Ts: 0.1



# Simulation in LabVIEW



# Code

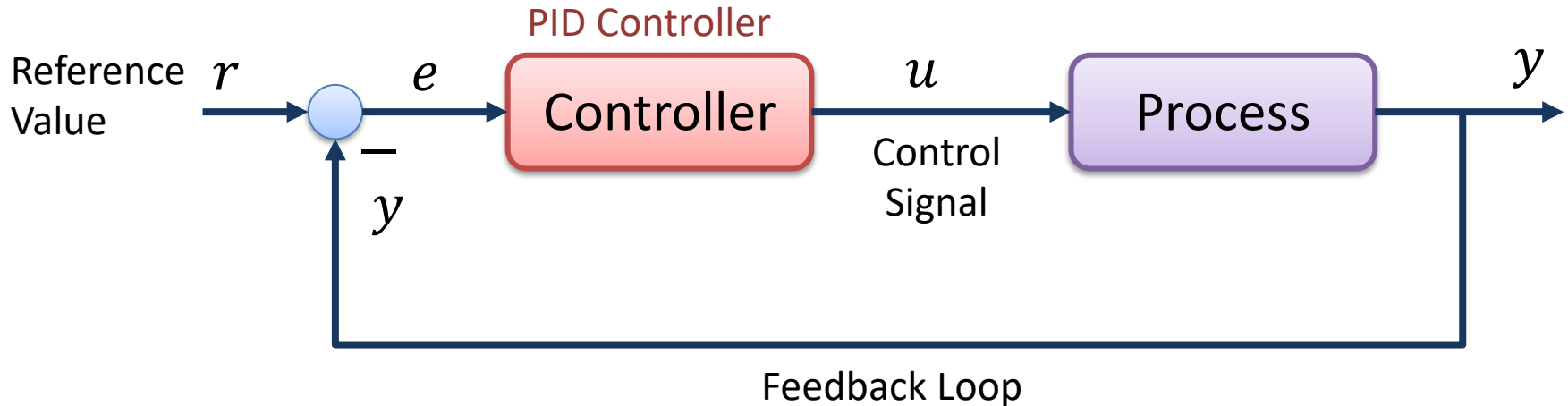




# PID Controller

# Control System

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# PID Controller

$$u(t) = \underbrace{K_p e}_{\text{P}} + \underbrace{\frac{K_p}{T_i} \int_0^t e d\tau}_{\text{I}} + \underbrace{K_p T_d \dot{e}}_{\text{D}}$$

Proportional Gain

Integral Time

Derivative Time

Tuning Parameters:

$K_p$

$T_i$

$T_d$



# PI Controller

Very often we just need a PI Controller:

$$u(t) = K_p e + \frac{K_p}{T_i} \int_0^t e d\tau$$

**Discrete** PI Controller that we can implement in different programming languages:

$$e_k = r_k - y_k$$

$$u_k = u_{k-1} + K_p (e_k - e_{k-1}) + \frac{K_p}{T_i} T_s e_k$$

# Discrete PI Controller

We start with the continuous PI Controller:

$$u(t) = K_p e + \frac{K_p}{T_i} \int_0^t e d\tau$$

We derive both sides in order to remove the Integral:

$$\dot{u} = K_p \dot{e} + \frac{K_p}{T_i} e$$

We can use the Euler Backward Discretization method:

$$\dot{x} \approx \frac{x(k) - x(k-1)}{T_s}$$

Where  $T_s$  is the Sampling Time

Then we get:

$$\frac{u_k - u_{k-1}}{T_s} = K_p \frac{e_k - e_{k-1}}{T_s} + \frac{K_p}{T_i} e_k$$

Finally, we get:

$$u_k = u_{k-1} + K_p (e_k - e_{k-1}) + \frac{K_p}{T_i} T_s e_k$$

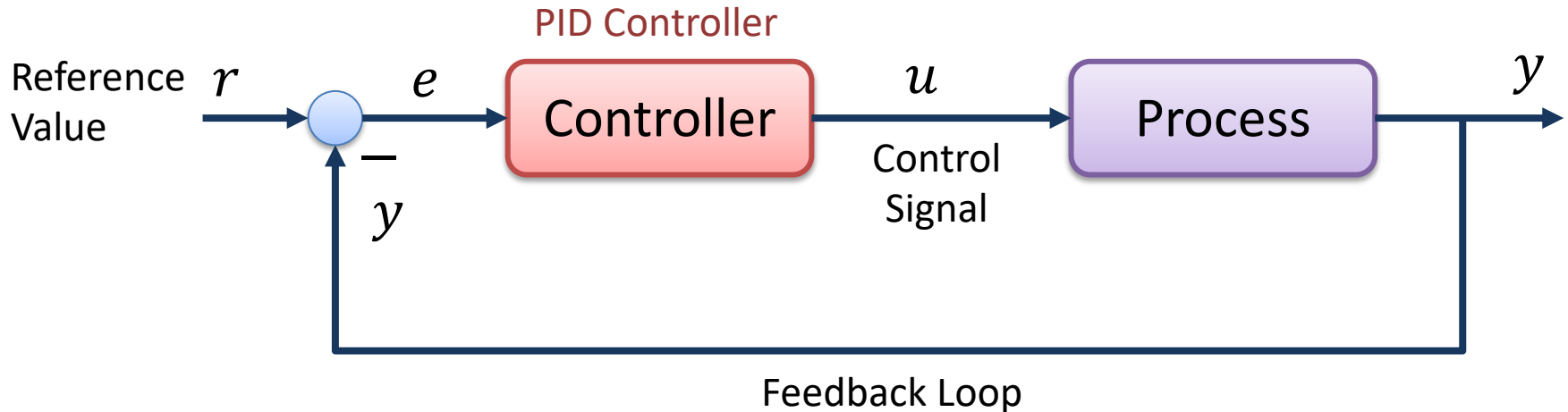
Where  $e_k = r_k - y_k$



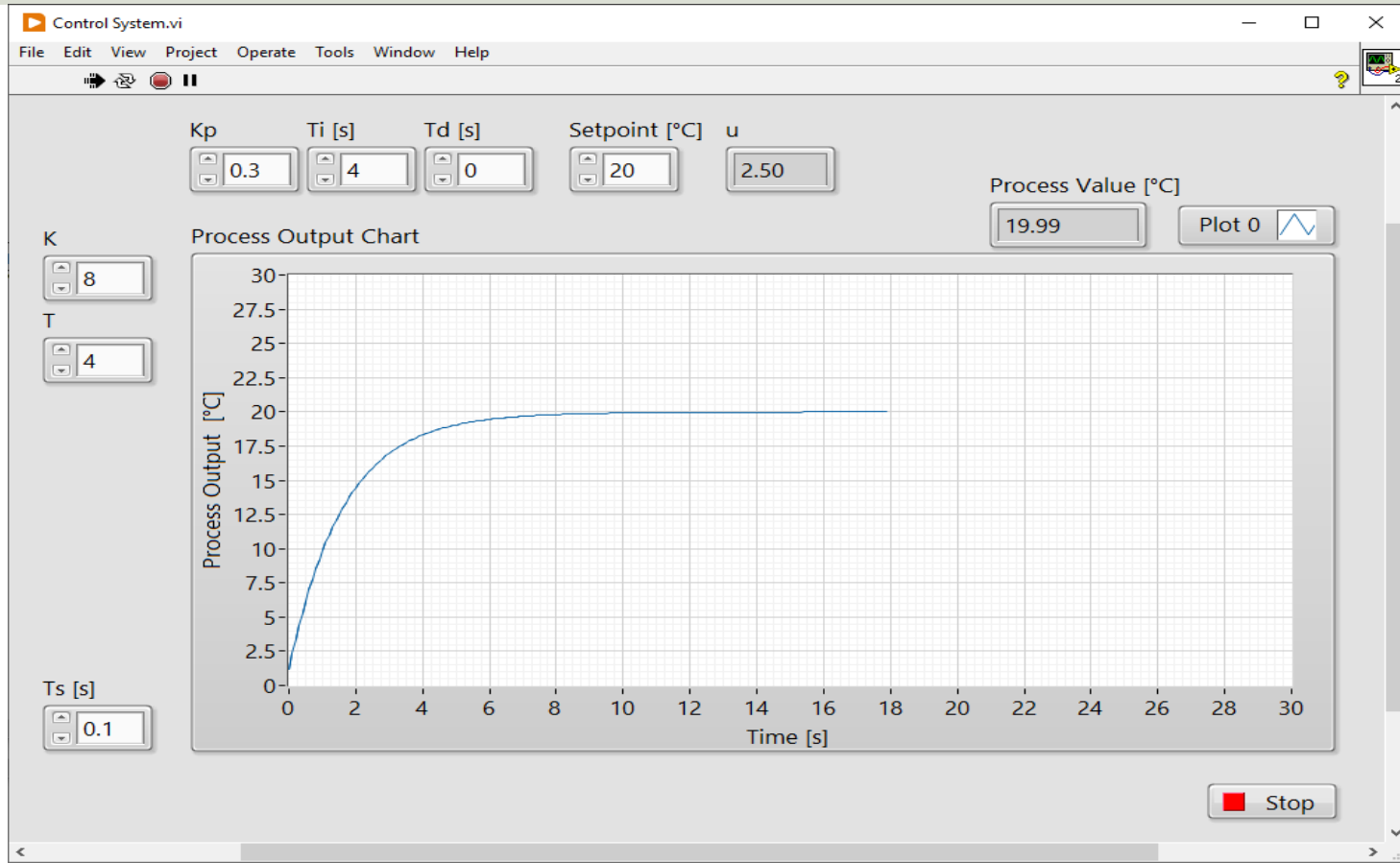
# Control System

# Control System

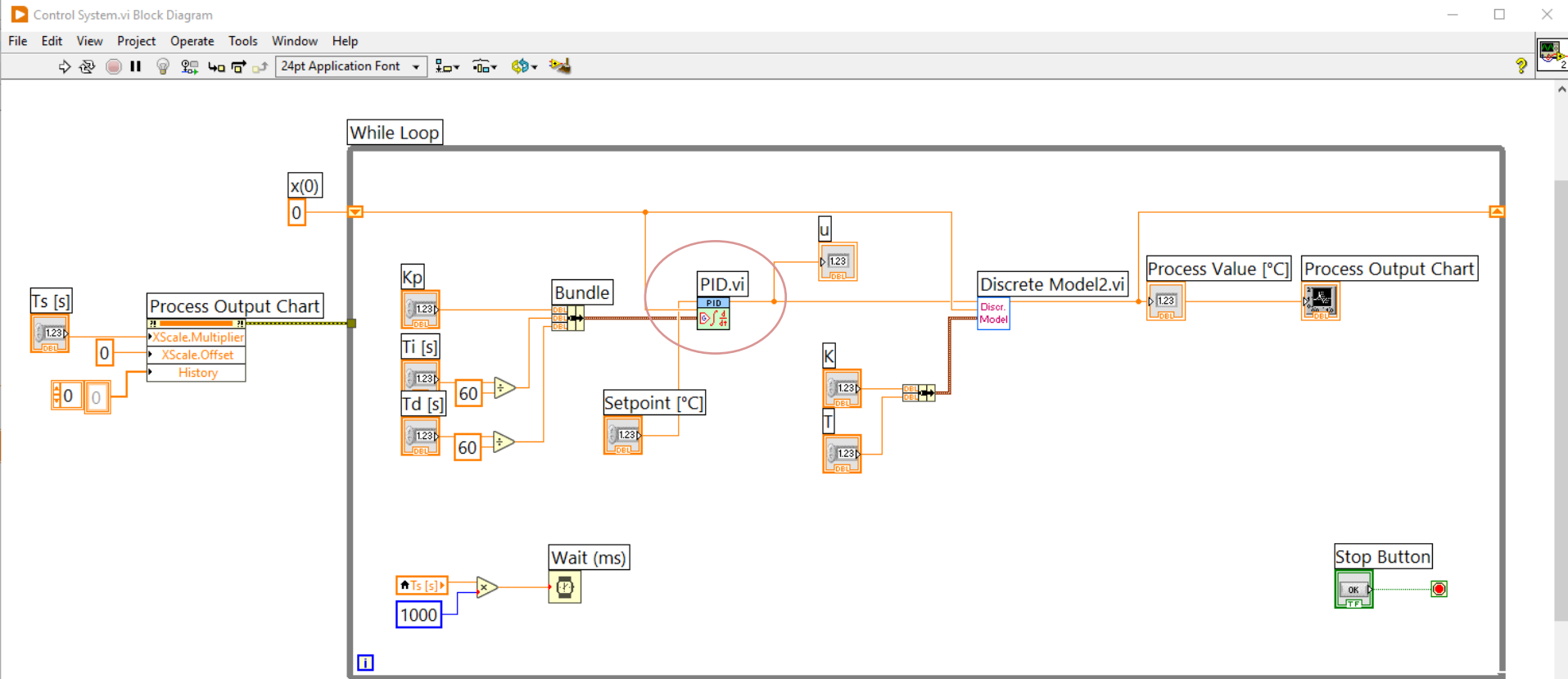
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# Control System in LabVIEW



# Built-in PID Controller



# Discrete PI Controller

Discrete PI Algorithm:

$$e_k = r_k - y_k$$
$$u_k = u_{k-1} + K_p(e_k - e_{k-1}) + \frac{K_p}{T_i} T_s e_k$$

Discrete PI Controller.vi Front Panel

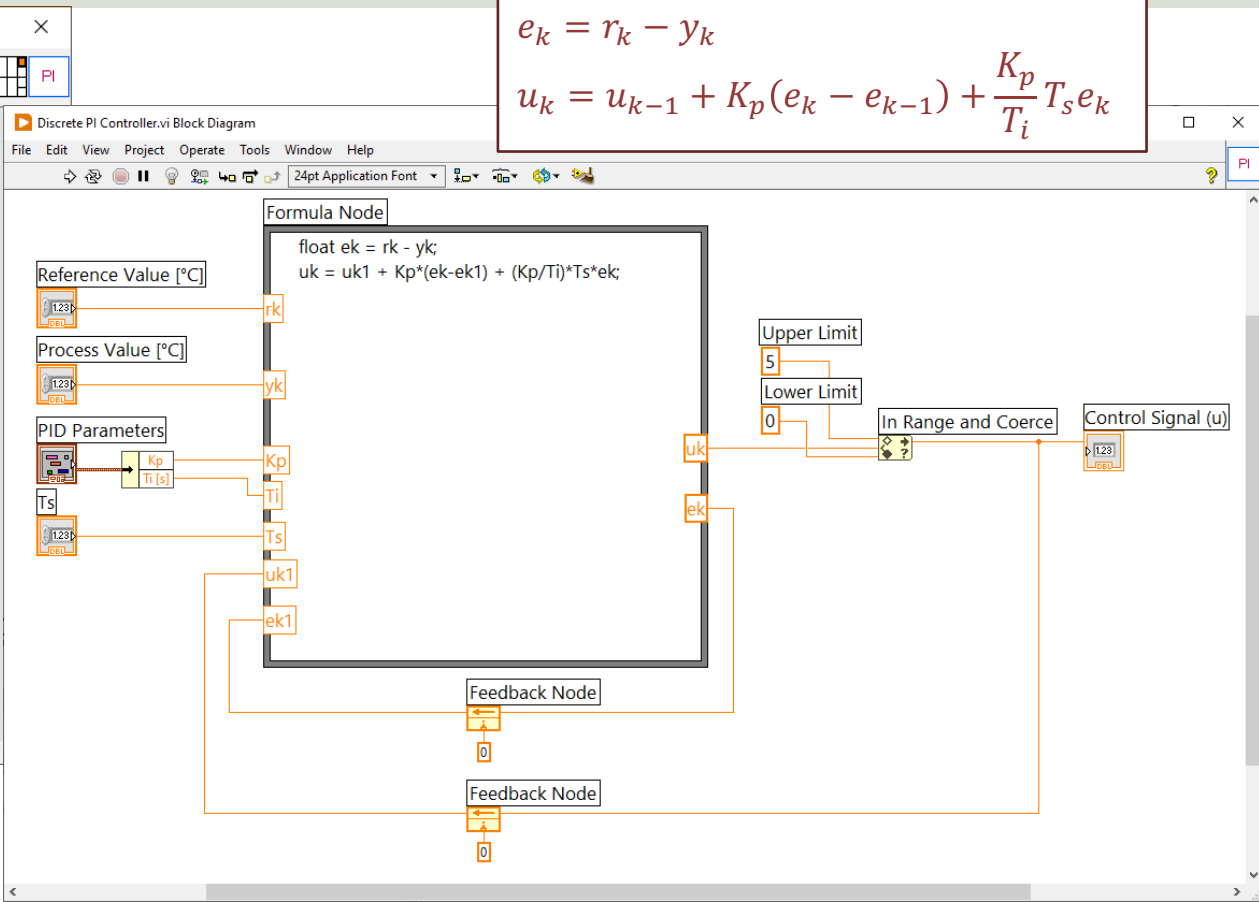
Process Value [°C]: 19.99

Reference Value [°C]: 20.00

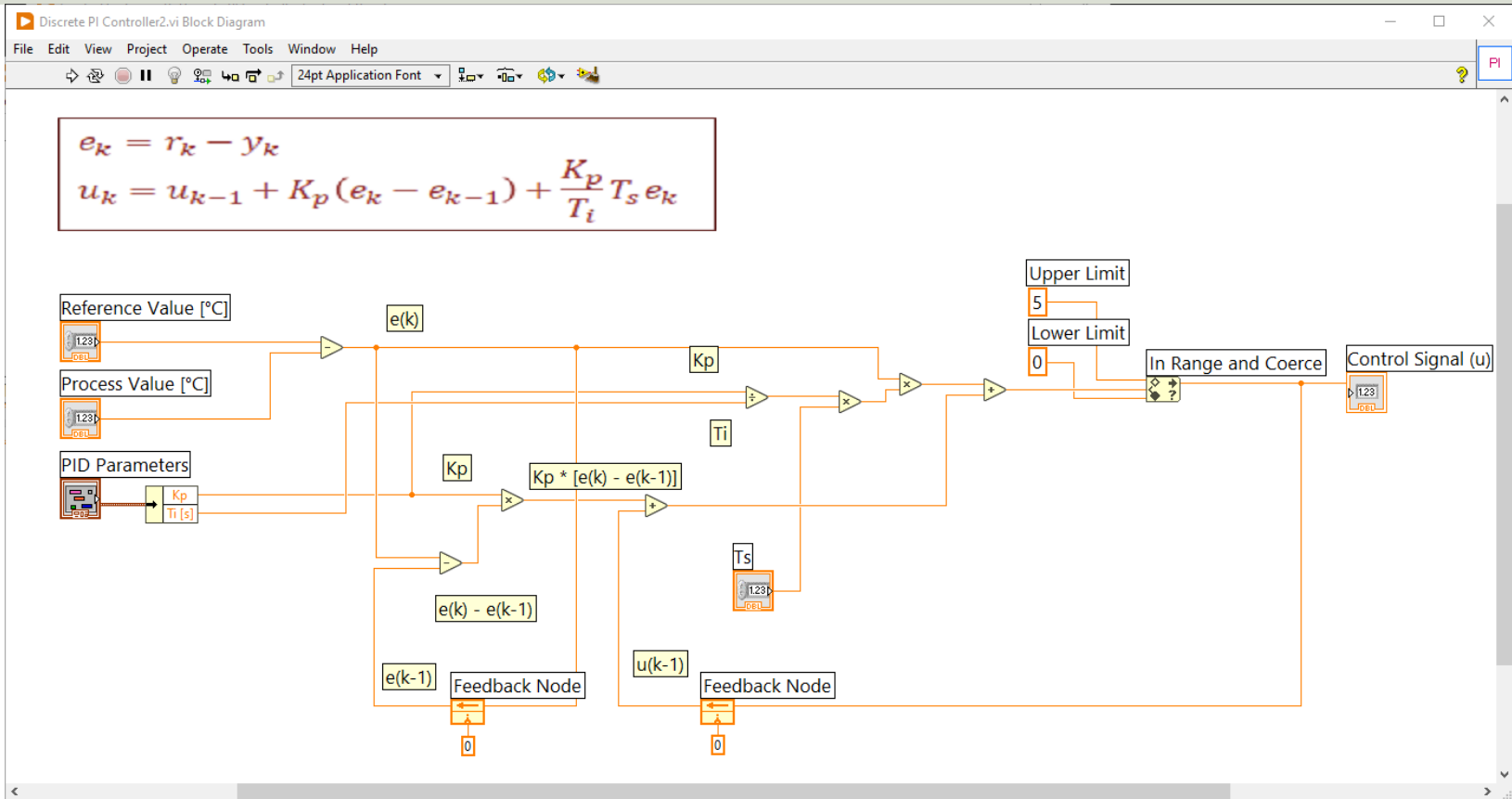
PID Parameters

- Kp: 0.5
- Ts: 4
- Ti: 0.1

Control Signal (u): 2.50

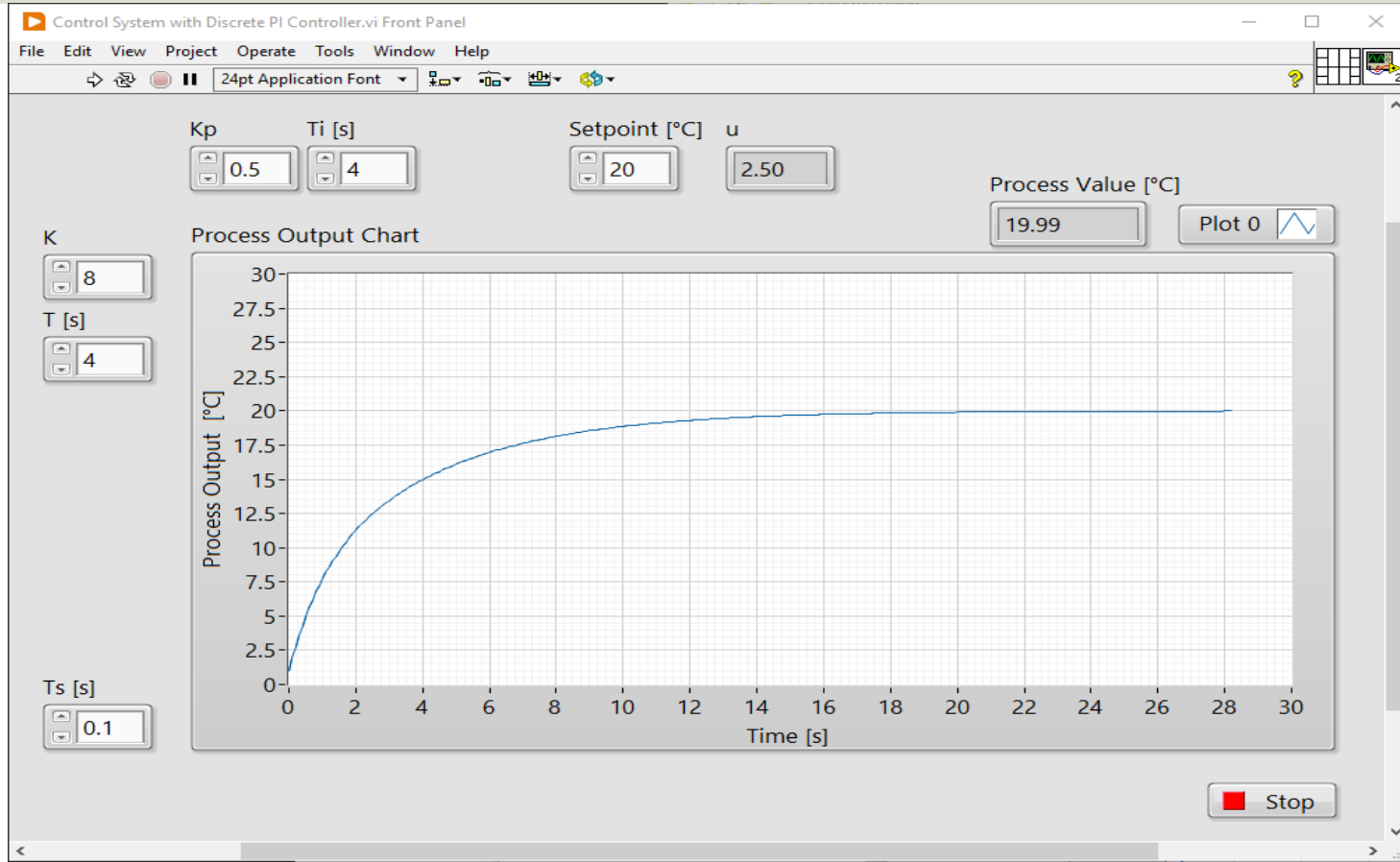


# Discrete PI Controller (Alternative Solution)

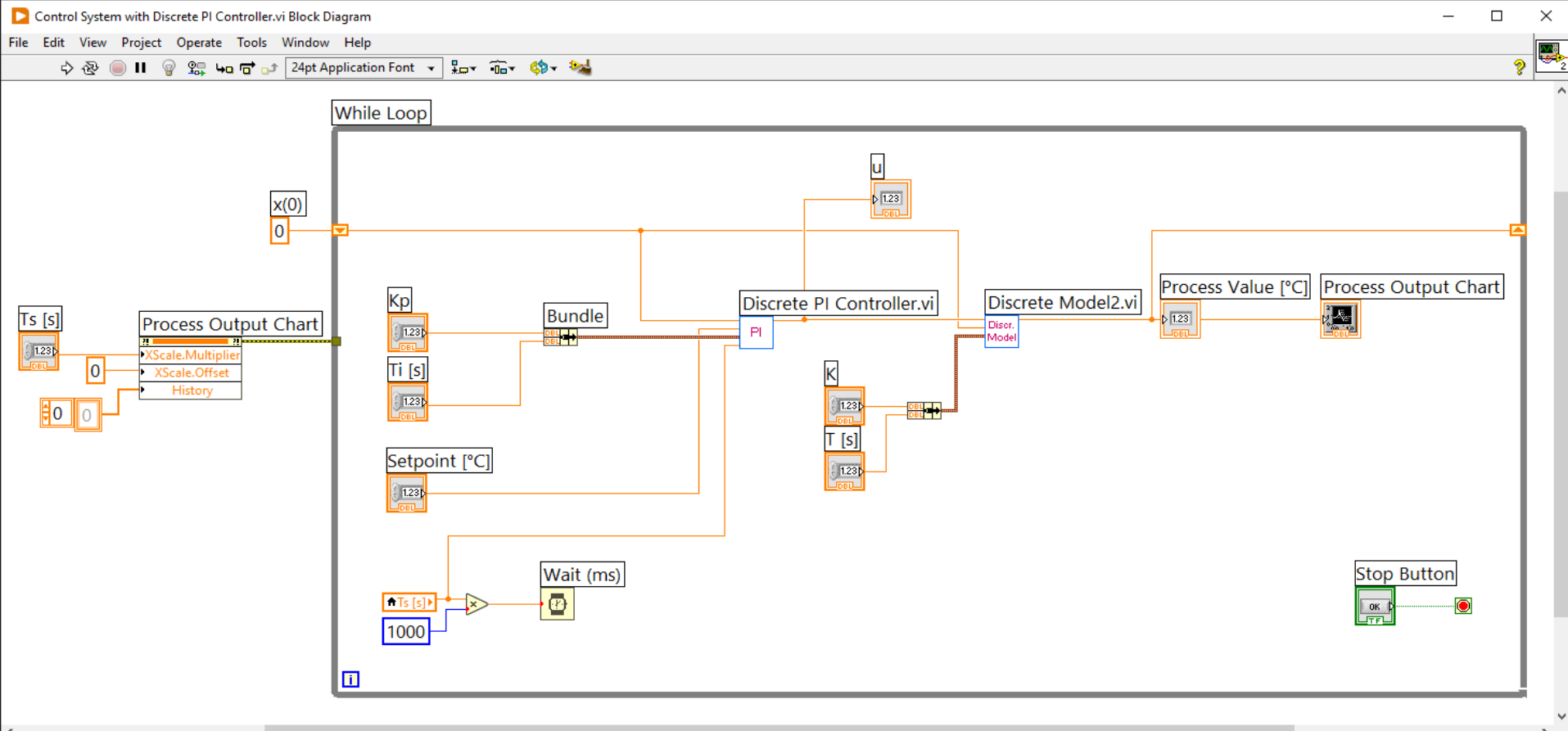




# Control System in LabVIEW



# Control System Code



# Summary

- A Basic Control System has been made using LabVIEW
- Lots of Improvements can be made, e.g.,:
  - Improve GUI
    - More Features/Functionality, More Intuitive and more user-friendly
  - Improve Code Structure, e.g., use a State Machine principle
  - Make a more robust PI(D) Controller
  - Use and Test with a more complicated Process/Model
  - Find better PI(D) Parameters using different Tuning methods, e.g., Ziegler-Nichols, Skogestad, etc.
  - Connect and Control a Real Process using a DAQ Device
  - Etc.

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